Message Passing for Decoding and Inference (\$21/25/26)

Recall from Tue/Thu:



$$G(x^{U}) = Q(Y_{1}|X_{1}) \cdots Q(Y_{U}|X_{U}) \Lambda[Hx^{U} = 0]$$

$$G_{1} \text{ m terms of noise vector} n^{U} = x^{U} \oplus y^{U} :$$

$$G(n^{U}) = P(n_{1}) \cdots P(n_{U}) \cdot \Lambda[Hn^{U} = Hy^{U}]$$

$$assuming T^{U} = X^{U} \oplus N^{U} \quad \text{i.i.d. noise}$$





$$\frac{|r_{fe}ene}{2} = \Pr(B=1|A=1) = \frac{\Pr(B=1,A=1)}{\sum \Pr(B=1,A=1)}$$

Lo enough to compute $\Pr(B=1,A=1) = \sum \Pr(e,b,r,1,p)$
magnal of B e,r,p product of local factors
How to guad having to first compute $\Pr(e,b,r,1,p)$ for all e,b,r,p^{2}

(3) <u>Statistical Physics</u>: Using model on lattice * one periode per site with states $x_i \in \{\pm 1\}$ * total energy $E[\{x_i\}] = \sum_{i=j}^{j} \frac{1}{2}(1-x_ix_j)$ energy cost J if host same Partition function at knoperature T: $\frac{1}{2} = \sum_{i=j}^{j} e^{-E[\{x_i\}]/T} = \sum_{i=j}^{j} \frac{1}{2}(1-x_ix_j)$ $\frac{1}{2} = \sum_{i=j}^{j} e^{-E[\{x_i\}]/T} = \sum_{i=j}^{j} \frac{1}{2}(1-x_ix_j)$ $\frac{1}{2} = \sum_{i=j}^{j} e^{-E[\{x_i\}]/T} = \sum_{i=j}^{j} \frac{1}{2}(1-x_ix_j)$



$$\frac{\text{Sum} - \text{product algorithm} ("belief propagation"):}{\text{Input}: Tackor gaph & factas $2f_i$ & integer T
() For all edges (x) - [fm] and all $x_i \in d_i$:
 $q_{i \rightarrow m}(x_i) \leftarrow l$
(2) For T steps:
Tor all edges (x) - [fm] and all $x_i \in d_i$:
 $r_{m \rightarrow i}(x_i) \leftarrow \sum_{i \neq j \neq i} fm(2x_i)_{i \neq i} fm(2x_i)_{i \neq i} fm(2x_i)_{i \neq i} fm(2x_i)_{i \neq i}$
Tor all edges (x) - [fm] and all $x_i \in d_i$:
 $for all edges (x) - [fm] and all $x_i \in d_i$:
 $q_{i \rightarrow m}(x_i) \leftarrow \sum_{i \neq j \neq i} fm(2x_i)_{i \neq i} fm(2x_$$$$

* Portition function: $Z = \sum_{x, N} G(x^N) = ? - 3 \text{ physics } [Z = \sum_{x;} G_i(x_i)]$ * Maximum: max $G(x^N) = ? - 0 \text{ Other decoding}$ x^N [Replace Z by max ~ "max - product" also ~ "mm-sum" also]

Outlook

What did we WOT cover? * Channels with memory * Multi-user information theory * Multi-user information theory * Move connections to inference, machine learning, etc. * How to decode barcode from Lecture 1 22

* Quantum information theory -> Mostertlath couse with Maris Ords & Quantum Computing -> Couses by Maris (BSC) + Ronald de Walf (MSC) * Connections to Gyptography -> Course by Chris Schaffrer

How to prepare for the exam? * Learning objectives @ homepage Courre manual NOT up to date !!! * Leature notes, homeworky problems from the ex. class * Dan't forget to prepare your chect sheet * Structure: mix of problems of type ()+(2) from HW

THANKS + SEE you AGAIN SOON o